



Chapter 24


Introduction to Spectrochemical Methods

Definition and Overview

- Spectroscopy:
A general term for the science that deals with various types of **electromagnetic radiation** (EMR) with *mater*.

P_0

 λ


 Sample
 b


 P

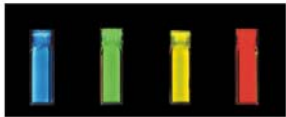
$$T = \frac{P}{P_0}$$

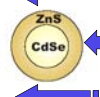
$$A = \log \frac{P_0}{P}$$


$$= -\log T$$

$A = f(b, C)_\lambda$ Absorption Spectroscopy

Optical Properties of Semiconductor Nanoparticles

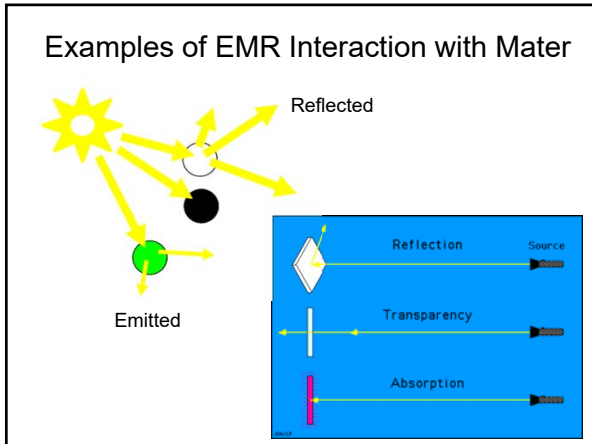

 2.3 nm 4.2 nm 4.8 nm 5.5 nm
 Larger Band Gap Smaller Band Gap
Courtesy of Bavendi and Coworkers.

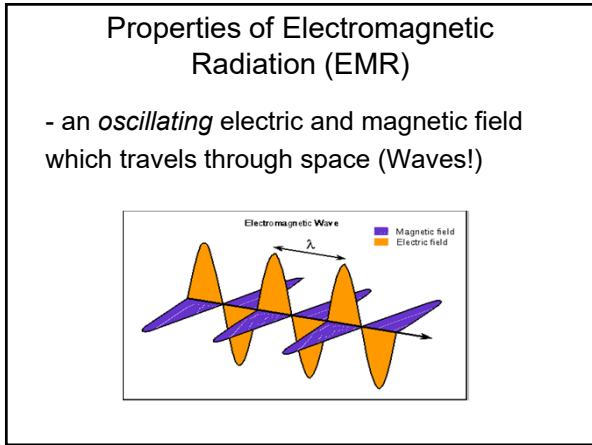

 ZnS
 CdSe


 UV Light

$I = f(C)$

Emission Spectroscopy

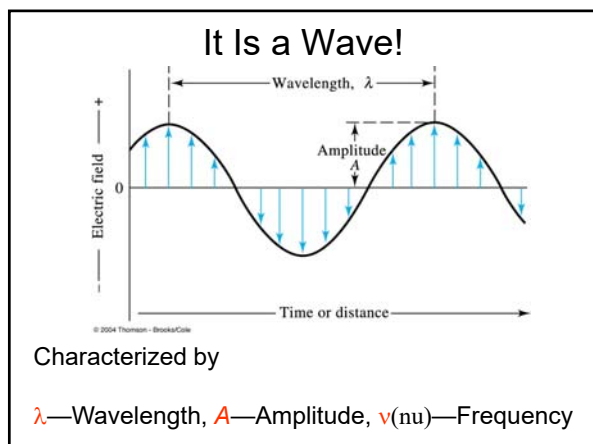




Also, EMR

--a discrete series of "particles" that have a specific energy but have no Mass (Particles!)

Waves + Particles



Wave Properties of EMR

The product of λ and ν is constant:

$$\lambda \times \nu = c$$

Since ν has units of sec^{-1} (hz) and λ has units of length,
their product, c , is the *velocity* of the wave:

- **in a vacuum**, all EMR travels at a velocity of:
 $2.99792458 \times 10^8 \text{ m/s}$ (= c)
("The Speed of Light")

$C = 3 \times 10^8 \text{ m/s} = 3 \times 10^{10} \text{ cm/s} = 3 \times 10^{17} \text{ nm/s} = 3 \times 10^{18} \text{ \AA/s}$

- Wavenumber

$$\bar{\nu} = 1/\lambda$$

–the number of waves per centimeter

$\bar{\nu}$ has the units of cm^{-1}

Propagation Velocity

- What happens as an EMR wave propagates from a vacuum into another medium?

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v unchanged; λ decreases; velocity decreases.

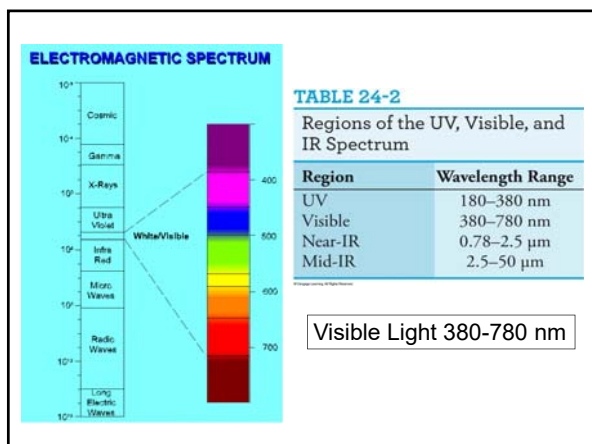
EMR Spectrum

Type of quantum change:	Change of spin	Change of orientation	Change of configuration	Change of electron distribution	Change of nuclear configuration		
	10^{-2}	1	100	10^6	10^8		
	10 m	100 cm	1 cm	100 μm	1000 nm		
	3 × 10 ⁶	3 × 10 ⁸	3 × 10 ¹⁰	3 × 10 ¹⁴	3 × 10 ¹⁶		
	10 ⁻¹	10 ⁻¹	10	10 ³	10 ⁷		
Type of spectroscopy:	NMR	ESR	Microwave	Infrared	Visible and ultraviolet	X-ray	γ-ray

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EMR covers a wide range of wavelengths and frequencies.

The Electromagnetic Spectrum



Particle Properties of EMR

- EMR: A beam of energetic particles (“photons”).
- Photon are “destroyed” after absorption by a sample.
- Energy of a photon is related to its frequency.

$$E = h\nu = h \frac{c}{\lambda} = hc\nu$$

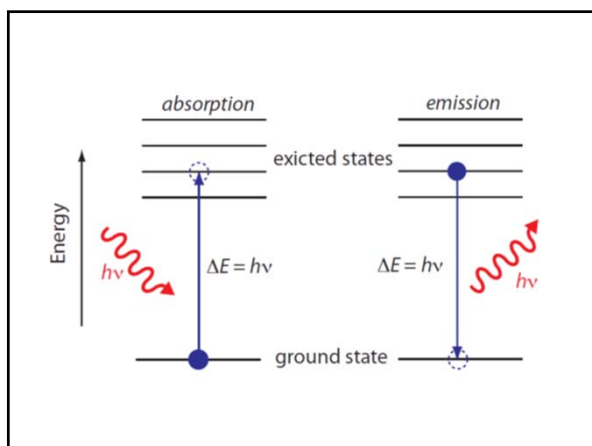
h is Plank’s constant
(6.63×10^{-34} J·s)

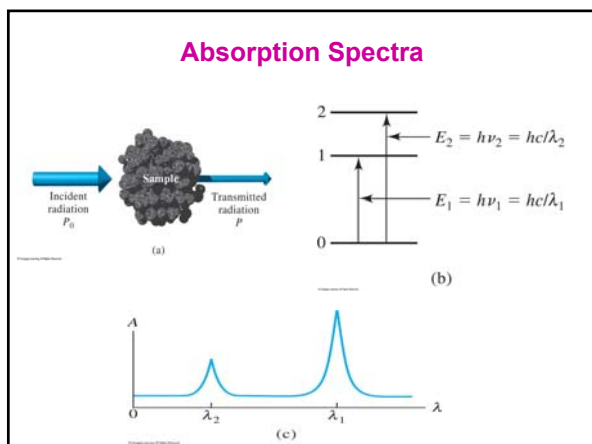
What is the energy of a photon from the sodium D line at 589 nm?

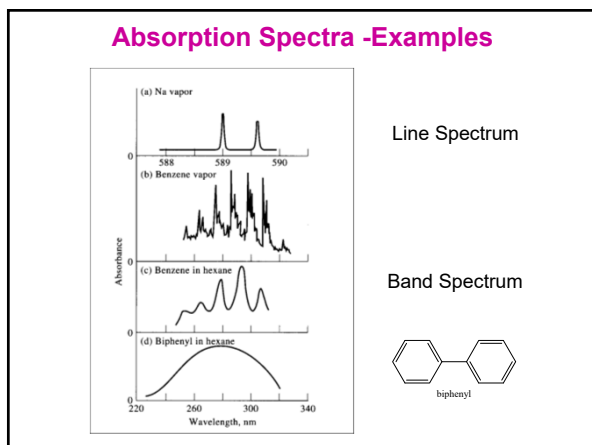
SOLUTION

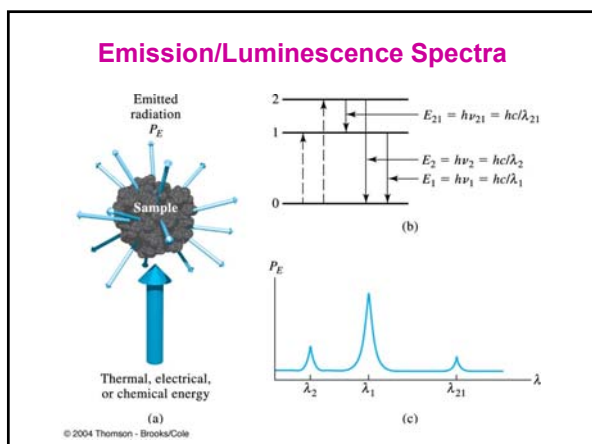
The photon’s energy is

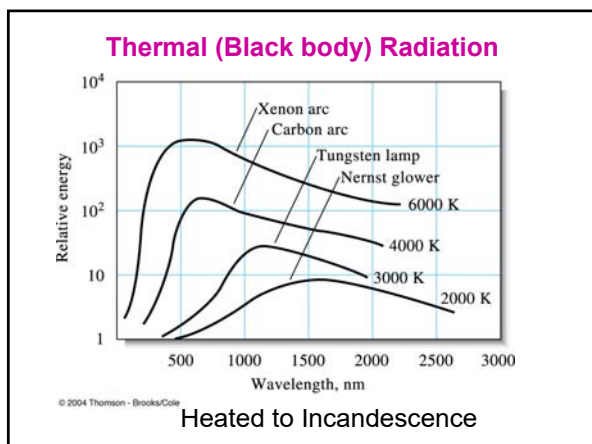
$$E = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(3.00 \times 10^8 \text{ m/s})}{589 \times 10^{-9} \text{ m}} = 3.37 \times 10^{-19} \text{ J}$$

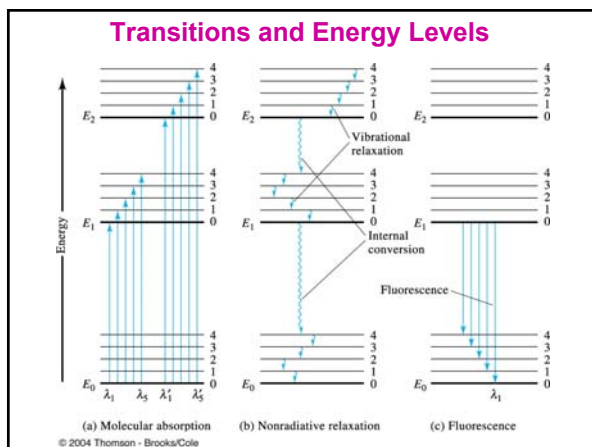


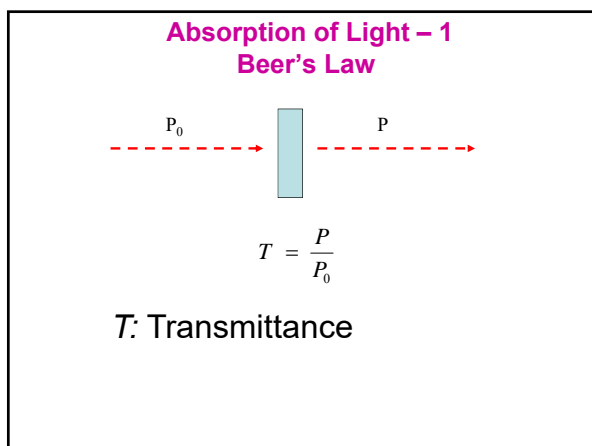




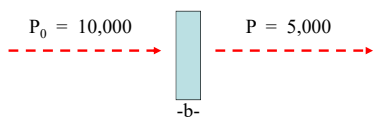






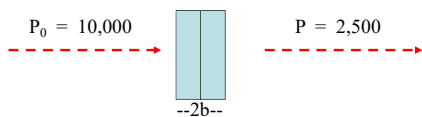


Absorption of Light – 2 Beer's Law



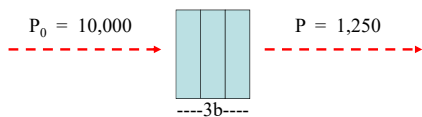
$$T = \frac{P}{P_0} = \frac{5000}{10000} = 0.5$$

Absorption of Light – 3 Beer's Law



$$T = \frac{P}{P_0} = \frac{2500}{10000} = 0.25$$

Absorption of Light – 4 Beer's Law



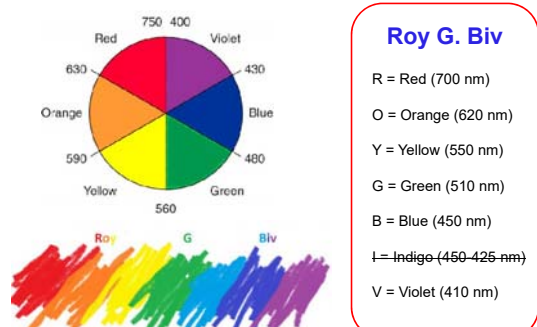
$$T = \frac{P}{P_0} = \frac{1250}{10000} = 0.125$$

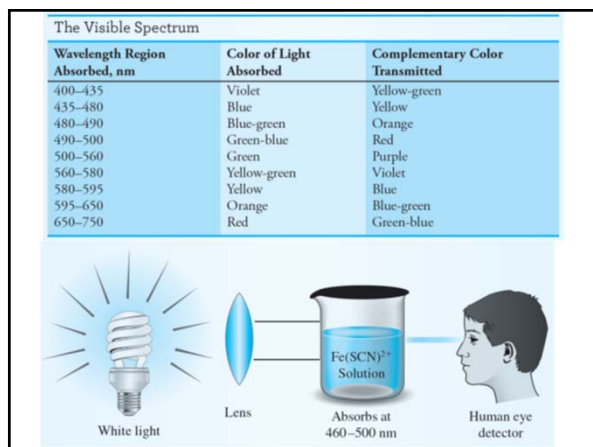
$$A = -\log T = -\log \frac{P}{P_0}$$

$A = abc$

A = absorbance
 a = absorptivity
 b = thickness
 c = concentration

Color Wheel Complementary Colors





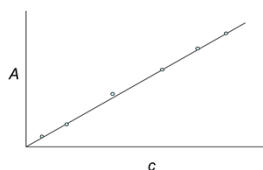
Beer's Law

$$A^\lambda = -\log T^\lambda = -\log \left[\frac{P}{P_0} \right]_\lambda$$

$$A^\lambda = a_\lambda bc = \epsilon_\lambda bc$$

A = absorbance
 a = absorptivity
 b = thickness
 c = concentration
 ϵ = molar absorptivity

When b in cm, c in mol/L, a is called molar absorptivity and is given the special symbol ϵ (in L/(mol cm))



Beer's Law for Mixture-Additive

At any given wavelength of EMR absorption:

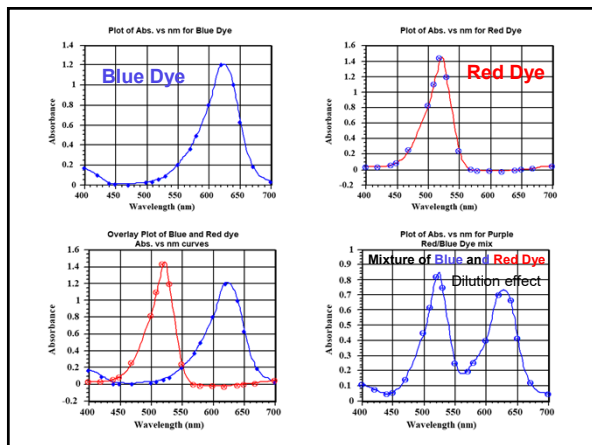
$A^\lambda = \epsilon^\lambda bc$, for a mixture with n components,

the total A_{Total}^λ :

$$A_{Total}^\lambda = A_1^\lambda + A_2^\lambda + \dots + A_n^\lambda = \sum_{i=1}^n A_i^\lambda = \sum_{i=1}^n \epsilon_i^\lambda bc_i$$

Example:

Mixture of Co(II), Cr(III), Ni(II), Cu(II)



Example:

The concentrations of Fe^{3+} and Cu^{2+} in a mixture are determined following their reaction with hexacyanoruthenate (II), $\text{Ru}(\text{CN})_6^{4-}$, which forms a purple-blue complex with Fe^{3+} ($\lambda_{\text{max}} = 550 \text{ nm}$) and a pale-green complex with Cu^{2+} ($\lambda_{\text{max}} = 396 \text{ nm}$). The molar absorptivities ($\text{M}^{-1} \text{ cm}^{-1}$) for the metal complexes at the two wavelengths are summarized in the following table.

	ϵ_{550}	ϵ_{396}
Fe^{3+}	9970	84
Cu^{2+}	34	856

When a sample that contains Fe^{3+} and Cu^{2+} is analyzed in a cell with a pathlength of 1.00 cm, the absorbance at 550 nm is 0.183 and the absorbance at 396 nm is 0.109. What are the molar concentrations of Fe^{3+} and Cu^{2+} in the sample?

Solution:

$$A_{550} = 0.183 = 9970C_{\text{Fe}} + 34C_{\text{Cu}}$$

$$A_{396} = 0.109 = 84C_{\text{Fe}} + 856C_{\text{Cu}}$$

To determine C_{Fe} and C_{Cu} we solve the first equation for C_{Cu}

$$C_{\text{Cu}} = \frac{0.183 - 9970C_{\text{Fe}}}{34}$$

and substitute the result into the second equation.

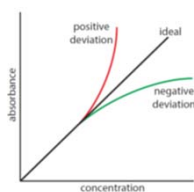
$$\begin{aligned} 0.109 &= 84C_{\text{Fe}} + 856 \times \frac{0.183 - 9970C_{\text{Fe}}}{34} \\ &= 4.607 - (2.51 \times 10^3)C_{\text{Fe}} \end{aligned}$$

Solving for C_{Fe} gives the concentration of Fe^{3+} as 1.8×10^{-5} M. Substituting this concentration back into the equation for the mixture's absorbance at 396 nm gives the concentration of Cu^{2+} as 1.3×10^{-4} M.

Limitations to Beer's law**1. Concentration Limit: ≤ 0.10 M.**

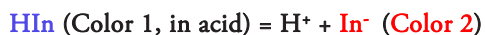
(a) At higher c the individual particles of analyte no longer are independent of each other—changing the ϵ value.

(b) The ϵ value depends on the solution's refractive index that varies with the c .



Limitations to Beer's law**2. Chemical limitations when chemical reactions occur.**

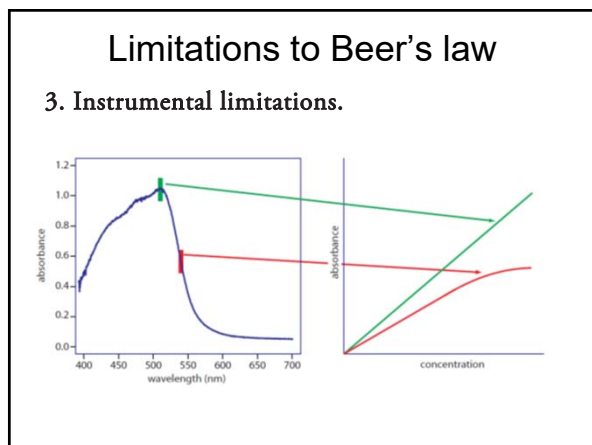
Example: different c of a weak acid dissociation in water (acid-base indicators)



Increase total $[\text{HIn}]_{\text{total}}$, $[\text{HIn}]$ and $[\text{In}^-]$
increase non-linearly.

TABLE 24-4
Absorbance Data for Several Concentrations of the Indicator in Example 24-5

$[HIn], M$	$[HIn]$	$[In^-]$	A_{430}	A_{570}
2.00×10^{-5}	0.88×10^{-5}	1.12×10^{-5}	0.236	0.073
4.00×10^{-5}	2.22×10^{-5}	1.78×10^{-5}	0.381	0.175
8.00×10^{-5}	5.27×10^{-5}	2.73×10^{-5}	0.596	0.401
12.0×10^{-5}	8.52×10^{-5}	3.48×10^{-5}	0.771	0.640
16.0×10^{-5}	11.9×10^{-5}	4.11×10^{-5}	0.922	0.887



- Beer's Law Should be used Only for a Single Wavelength Incident Light.
- It is the basis of quantitative Analysis of Absorption Spectroscopy.

Photometric Titrations

- A photometric titration curve is a plot of absorbance as a function of the volume of titrant.
- The spectrometer detects the color change of an indicator allowing the endpoint to be accurately determined.
- For example: titration of an acid and base using phenolphthalein clear \rightarrow pink

