

Chapters 19 & 20

Applications of Standard Electrode Potentials & Redox Titrations

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- Part 1: Calculating Potentials of Electrochemical Cells (Examples 19-1~10)--Nernst equation for half-cells and chemical cells

(1) For an half cell: Ox + ne = Red

$$E = E^0 + \frac{RT}{nF} \ln \frac{a_{\text{Ox}}}{a_{\text{Red}}} = E^0 + \frac{0.0592}{n} \log \frac{a_{\text{Ox}}}{a_{\text{Red}}} \quad (@298\text{ K})$$

(2) For an electrochemical cell:

$$E_{\text{cell}} = E_{\text{cathode(+, right)}} - E_{\text{anode(-, left)}}; \quad \Delta G = -nF\Delta E_{\text{cell}}$$

$$\Delta E = \Delta E^0 - \frac{RT}{nF} \ln Q = \Delta E^0 - \frac{0.0592}{n} \log Q \text{ at } 298\text{ K (25 }^\circ\text{C)}$$

(3) At chemical equilibrium:

$$E_{\text{cell}} = E_{\text{cathode(+, right)}} - E_{\text{anode(-, left)}} = 0$$

When the reaction reaches equilibrium

$$\ln K_{\text{eq}} = \frac{nF\Delta E^0}{RT}, \text{ or } \log K_{\text{eq}} = \frac{n\Delta E^0}{0.0592} \text{ (at 298K)}$$

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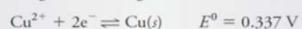
Example 19-1

Calculate the thermodynamic potential of the following cell and the free energy change associated with the cell reaction:



Solution

The two half-reactions and standard potentials are



The electrode potentials are

$$E_{\text{Ag}^+/\text{Ag}} = 0.799 - 0.0592 \log \frac{1}{0.0200} = 0.6984\text{ V}$$

$$E_{\text{Cu}^{2+}/\text{Cu}} = 0.337 - \frac{0.0592}{2} \log \frac{1}{0.0200} = 0.2867\text{ V}$$

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$$E_{\text{cell}} = E_{\text{right}} - E_{\text{left}} = E_{\text{Ag}^+/\text{Ag}} - E_{\text{Cu}^{2+}/\text{Cu}} = 0.6984 - 0.2867 = +0.412 \text{ V}$$

The free energy change ΔG for the reaction $\text{Cu}(s) + 2\text{Ag}^+ \rightleftharpoons \text{Cu}^{2+} + 2\text{Ag}(s)$ is found from

(1 calorie = 4.18 Joules)

$$\Delta G = -nFE_{\text{cell}} = -2 \times 96485 \text{ C} \times 0.412 \text{ V} = -79,503 \text{ J} (18.99 \text{ kcal})$$

EXAMPLE 19-2

Calculate the potential for the cell



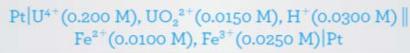
$$E_{\text{Ag}^+/\text{Ag}} = 0.6984 \text{ V} \quad \text{and} \quad E_{\text{Cu}^{2+}/\text{Cu}} = 0.2867 \text{ V}$$

$$E_{\text{cell}} = E_{\text{right}} - E_{\text{left}} = E_{\text{Cu}^{2+}/\text{Cu}} - E_{\text{Ag}^+/\text{Ag}} = 0.2867 - 0.6984 = -0.412 \text{ V}$$

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EXAMPLE 19-3

Calculate the potential of the following cell and indicate the reaction that would occur spontaneously if the cell were short-circuited (see Figure 19-1).



Solution

The two half-reactions are



The electrode potential for the right-hand electrode is

$$\begin{aligned} E_{\text{right}} &= 0.771 - 0.0592 \log \frac{[\text{Fe}^{2+}]}{[\text{Fe}^{3+}]} \\ &= 0.771 - 0.0592 \log \frac{0.0100}{0.0250} = 0.771 - (-0.0236) \\ &= 0.7946 \text{ V} \end{aligned}$$

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The electrode potential for the left-hand electrode is

$$\begin{aligned} E_{\text{left}} &= 0.334 - \frac{0.0592}{2} \log \frac{[\text{U}^{4+}]}{[\text{UO}_2^{2+}][\text{H}^+]^4} \\ &= 0.334 - \frac{0.0592}{2} \log \frac{0.200}{(0.0150)(0.0300)^4} \\ &= 0.334 - 0.2136 = 0.1204 \text{ V} \end{aligned}$$

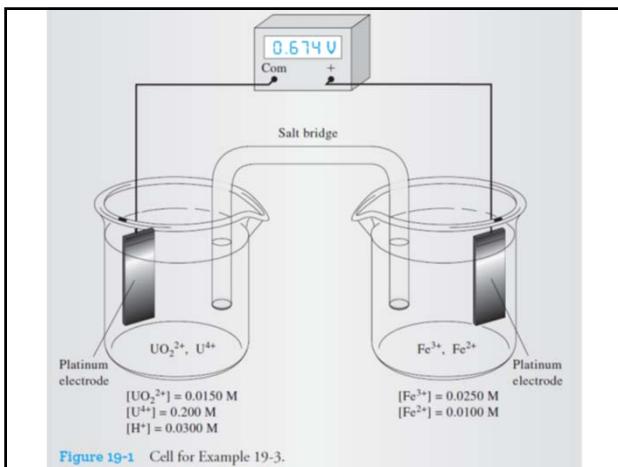
and

$$E_{\text{cell}} = E_{\text{right}} - E_{\text{left}} = 0.7946 - 0.1204 = 0.6742 \text{ V}$$

The positive sign means that the spontaneous reaction is the oxidation of U^{4+} on the left and the reduction of Fe^{3+} on the right, or



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EXAMPLE 19-4

Calculate the cell potential for



Solution

The two half-reactions and their corresponding standard electrode potentials are (see Table 18-1).



$$E_{\text{right}} = 0.000 - \frac{0.0592}{2} \log \frac{P_{\text{H}_2}}{[\text{H}^+]^2} = -\frac{0.0592}{2} \log \frac{0.800}{(0.0200)^2}$$

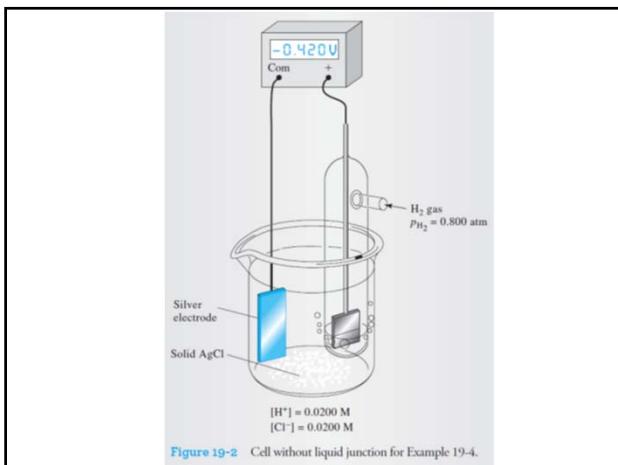
$$= -0.0977 \text{ V}$$

$$E_{\text{left}} = 0.222 - 0.0592 \log [\text{Cl}^-] = 0.222 - 0.0592 \log 0.0200$$

$$= 0.3226 \text{ V}$$

$$E_{\text{cell}} = E_{\text{right}} - E_{\text{left}} = -0.0977 - 0.3226 = -0.420 \text{ V}$$

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EXAMPLE 19-10

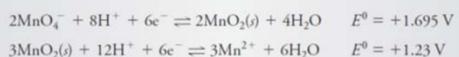
Calculate the equilibrium constant for the reaction



Comproportionation vs Disproportionation

Solution

In Appendix 5, we find



$$\frac{6(1.695 - 1.23)}{0.0592} = \log \frac{[\text{H}^+]^{12}}{[\text{MnO}_4^-]^2[\text{Mn}^{2+}]^3[\text{H}^+]^8}$$

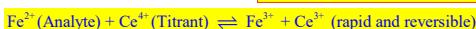
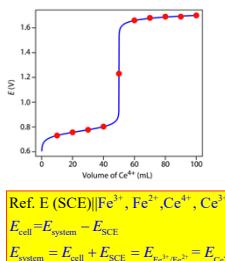
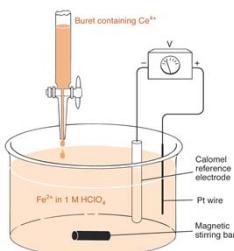
$2 \text{O}_2^- + 2 \text{H}^+ \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$

$$47.1 = \log \frac{[\text{H}^+]^4}{[\text{MnO}_4^-]^2[\text{Mn}^{2+}]^3} = \log K_{\text{eq}}$$

$$K_{\text{eq}} = \text{antilog } 47.1 = 1 \times 10^{47}$$

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Part 2: Constructing Redox Titration Curves



Reaction is rapid and reversible, hence at equilibrium

During the entire titration pro-

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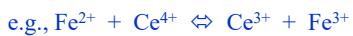
Calculation of Equivalence Potential

For $Ox_1 + n_{Ox_1} e \rightleftharpoons Red_1$

$$\text{Ox}_2 + n_{\text{Ox}_2} \text{e} \rightleftharpoons \text{Red}_2$$

$$\text{Ox}_l + \text{Red}_r \rightleftharpoons \text{Red}_l + \text{Ox}_r$$

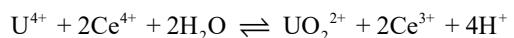
$$E_{\text{eq}} = \frac{n_{\text{Ox}_1} E^0_{\text{Ox}_1/\text{Red}_1} + n_{\text{Ox}_2} E^0_{\text{Ox}_2/\text{Red}_2}}{n_{\text{Ox}_1} + n_{\text{Ox}_2}}$$



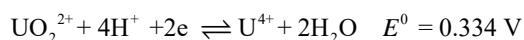
$$E_{\text{eq}} = \frac{n_{\text{Fe}} E_{\text{Fe}}^0 + n_{\text{Ce}} E_{\text{Ce}}^0}{n_{\text{Fe}} + n_{\text{Ce}}} = \frac{1 \cdot 1.44 + 1 \cdot 0.68}{2} = 1.06 \text{ V}$$

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However:



in 1.0 M H₂SO₄

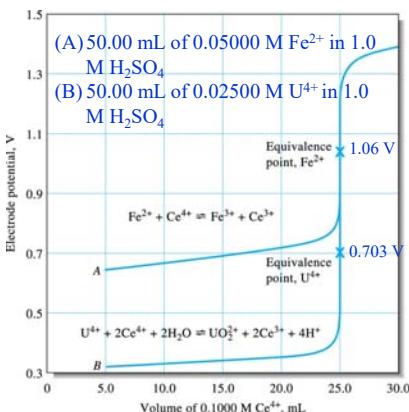


$$E_{\text{eq}} = \frac{2E_{\text{UO}_2^{2+}/\text{U}^{4+}}^0 + E_{\text{Ce}^{4+}/\text{Ce}^{3+}}^0}{3} + \frac{0.0592}{3} \log[\text{H}^+]^4$$

$$= \frac{2 \times 0.334 + 1.44}{3} + \frac{0.0592}{3} \log (1.0)^4 = 0.703 \text{ V}$$

E_{eq} is pH dependent. * with dilution effect.

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Redox Titration Curve

EXAMPLE 1: 50.00 mL of 0.0500 M Fe²⁺ is titrated with 0.1000 M Ce⁴⁺ in a medium that is 1.0 M in H₂SO₄. How many mLs of Ce⁴⁺ are required to reach to the equivalence point,?



At equivalence point,

$$n_{\text{Ce}^{4+}} = n_{\text{Fe}^{2+}}; (CV)_{\text{Ce}^{4+}} = (CV)_{\text{Fe}^{2+}}$$

$$0.1000 \cdot V_{\text{Ce}^{4+}} = (50.00 \cdot 0.0500)_{\text{Fe}^{2+}}$$

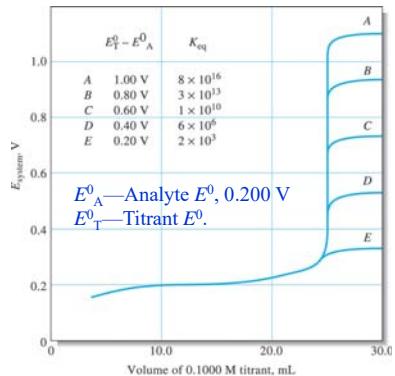
$$V_{\text{Ce}^{4+}} = 25.00 \text{ mL}$$

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Effect of Variables on Redox Titration Curves

- E_{system} is usually independent of dilution → Redox titration curves are usually independent of analyte and titrant concentrations—**Different from** neutralization, precipitation and complexation titrations.
 - The larger the equilibrium constants or the standard ΔE^0 ($\log K_{\text{eq}} = n\Delta E^0 / 0.0592$), the greater the change in equivalence-point region—**Similar** to other types of titrations.

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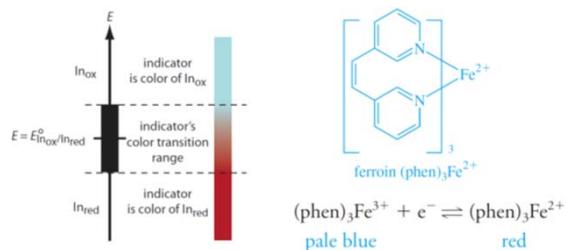


Effect of titrant electrode potential on reaction completeness.

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Oxidation/Reduction Indicators

- General redox indicators—substances change color upon redox reaction, which is dependent only on the potential of the titration system.



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General Redox Indicators

$$In_{ox} + ne \rightleftharpoons In_{red} \quad E = E_{In_{ox}/In_{red}}^0 + \frac{0.0592}{n} \log \frac{[In_{ox}]}{[In_{Red}]}$$

The color change is seen when $\frac{[In_{ox}]}{[In_{Red}]} \leq \frac{1}{10}$

changes to $\frac{[In_{ox}]}{[In_{Red}]} \geq \frac{10}{1}$ (overall change 100 times)

$$E = E_{In_{ox}/In_{red}}^0 \pm \frac{0.0592}{n}$$

$0.118/n$ V is needed for the E_{system} change.

Many indicators, $n = 2, 59$ mV E_{system} change sufficient.

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TABLE 19-3
Selected Oxidation/Reduction Indicators*

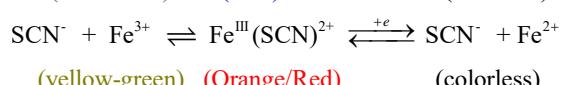
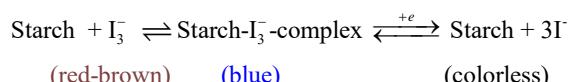
Indicator	Color		Transition Potential, V	Conditions
	Oxidized	Reduced		
5-Nitro-1,10-phenanthroline iron(II) complex	Pale blue	Red-violet	+1.25	1 M H ₂ SO ₄
2,3'-Diphenylamine dicarboxylic acid	Blue-violet	Colorless	+1.12	7-10 M H ₂ SO ₄
1,10-Phenanthroline iron(II) complex	Pale blue	Red	+1.11	1 M H ₂ SO ₄
5-Methyl 1,10-phenanthroline iron(II) complex	Pale blue	Red	+1.02	1 M H ₂ SO ₄
Erioglaucin A	Blue-red	Yellow-green	+0.98	0.5 M H ₂ SO ₄
Diphenylamine sulfonic acid	Red-violet	Colorless	+0.85	Dilute acid
Diphenylamine	Violet	Colorless	+0.76	Dilute acid
p-Ethoxychrysoidine	Yellow	Red	+0.76	Dilute acid
Methylene blue	Blue	Colorless	+0.53	1 M acid
Indigo tetrasulfonate	Blue	Colorless	+0.36	1 M acid
Phenosafanine	Red	Colorless	+0.28	1 M acid

*Data in part from I. M. Kolthoff and V. A. Stenger, *Volumetric Analysis*, 2nd ed., Vol. 1, p. 140.

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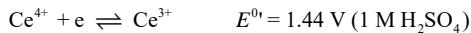
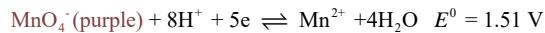
Oxidation/Reduction Indicators

- Specific indicators: (1) Starch for I₃⁻, (2) SCN⁻ (thiocyanate) for Fe(III)
- I₂ + I⁻ = I₃⁻ (triiodide ion)



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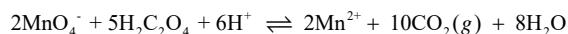
The Strong Oxidants - Potassium Permanganate and Cerium (IV)



Reactions are in strong acidic media.

MnO_4^- (purple) is a self-indicator.

Can be standardized with oxalate:



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TABLE 20-3

Some Common Oxidants Used as Standard Solutions

Reagent and Formula	Reduction Product	Standard Potential, V	Standardized With	Indicator*	Stability†
Potassium permanganate, KMnO_4	Mn^{2+}	1.51‡	$\text{Na}_2\text{C}_2\text{O}_4$, Fe, As_2O_3	MnO_4^-	(b)
Potassium bromate, KBrO_3	Br^-	1.44‡	KBrO_3	(1)	(a)
Cerium(IV), Ce^{4+}	Ce^{3+}	1.44‡	$\text{Na}_2\text{C}_2\text{O}_4$, Fe, As_2O_3	(2)	(a)
Potassium dichromate, $\text{K}_2\text{Cr}_2\text{O}_7$	Cr^{3+}	1.33‡	$\text{K}_2\text{Cr}_2\text{O}_7$, Fe	(3)	(a)
Iodine, I_2	I^-	0.536§	$\text{BaS}_2\text{O}_3 \cdot \text{H}_2\text{O}$, $\text{Na}_2\text{S}_2\text{O}_3$	starch	(c)

*(1) α -Naphthoflavone; (2) 1,10-phenanthroline iron(II) complex (ferroin); and (3) diphenylamine sulfonic acid.

†(a) indefinitely stable; (b) moderately stable, requires periodic standardization; and (c) somewhat unstable, requires frequent standardization.

‡ E° in 1 M H_2SO_4 .

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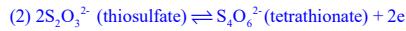
TABLE 20-5

Some Applications of Potassium Permanganate and Cerium(IV) Solutions

Substance Sought	Half-Reaction	Conditions
Sn	$\text{Sn}^{4+} \rightleftharpoons \text{Sn}^{2+} + 2\text{e}^-$	Prereduction with Zn
H_2O_2	$\text{H}_2\text{O}_2 \rightleftharpoons \text{O}_2(g) + 2\text{H}^+ + 2\text{e}^-$	
Fe	$\text{Fe}^{3+} \rightleftharpoons \text{Fe}^{2+} + \text{e}^-$	Prereduction with SnCl_2 or with Jones or Walden reductor
$\text{Fe}(\text{CN})_6^{4-}$	$\text{Fe}(\text{CN})_6^{4-} \rightleftharpoons \text{Fe}(\text{CN})_6^{3-} + \text{e}^-$	
V	$\text{VO}_2^{2+} + 3\text{H}_2\text{O} \rightleftharpoons \text{V}(\text{OH})_3^{+} + 2\text{H}^+ + \text{e}^-$	Prereduction with Bi amalgam or SO_2
Mo	$\text{Mo}^{6+} + 4\text{H}_2\text{O} \rightleftharpoons \text{MoO}_4^{2-} + 8\text{H}^+ + 3\text{e}^-$	Prereduction with Jones reductor
W	$\text{WO}_4^{2-} + 4\text{H}_2\text{O} \rightleftharpoons \text{W}O_2^{2-} + 8\text{H}^+ + 3\text{e}^-$	Prereduction with Zn or Cd
U	$\text{U}^{4+} + 2\text{H}_2\text{O} \rightleftharpoons \text{UO}_2^{2+} + 4\text{H}^+ + 2\text{e}^-$	Prereduction with Jones reductor
Tl	$\text{Tl}^{3+} + \text{H}_2\text{O} \rightleftharpoons \text{Tl}^{2+} + 2\text{H}^+ + \text{e}^-$	Prereduction with Jones reductor
$\text{H}_2\text{C}_2\text{O}_4$	$\text{H}_2\text{C}_2\text{O}_4 \rightleftharpoons 2\text{CO}_2 + 2\text{H}^+ + 2\text{e}^-$	
Mg, Ca, Zn, Co, Pb, Ag	$\text{H}_2\text{C}_2\text{O}_4 \rightleftharpoons 2\text{CO}_2 + 2\text{H}^+ + 2\text{e}^-$	
HNO_2	$\text{HNO}_2 + \text{H}_2\text{O} \rightleftharpoons \text{NO}_2^- + 3\text{H}^+ + 2\text{e}^-$	Sparingly soluble metal malates filtered, washed, and dissolved in acid; liberated oxalic acid titrated
K	$\text{K}_2\text{NaCr}(\text{NO}_2)_6 + 6\text{H}_2\text{O} \rightleftharpoons \text{Cr}^{3+} + 6\text{NO}_2^- + 12\text{H}^+ + 2\text{K}^+ + \text{Na}^+ + 11\text{e}^-$	15-min reaction time; excess KMnO_4 back-titrated
Na	$\text{U}^{4+} + 2\text{H}_2\text{O} \rightleftharpoons \text{UO}_2^{2+} + 4\text{H}^+ + 2\text{e}^-$	Precipitated as $\text{K}_2\text{NaCr}(\text{NO}_2)_6$ filtered and dissolved in KMnO_4 ; excess KMnO_4 back-titrated
		Precipitated as $\text{NaZn}(\text{UO}_2)_2(\text{OAc})_6$ filtered, washed, dissolved; U determined as above

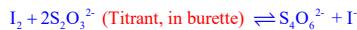
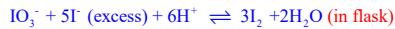
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Strong Reducing Agents— Fe(II) and thiosulfate



Standardized with potassium iodate:

<https://www.youtube.com/watch?v=tZYZZ9F7fM>



$1 \text{ mol } \text{IO}_3^- = 3 \text{ mol } \text{I}_2 = 6 \text{ mol } \text{S}_2\text{O}_3^{2-}$

Indicator: I_2 -starch (blue)



blue

colorless

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EXAMPLE 20-1

A solution of sodium thiosulfate was standardized by dissolving 0.1210 g KIO_3 (214.00 g/mol) in water, adding a large excess of KI , and acidifying with HCl. The liberated iodine required 41.64 mL of the thiosulfate solution to decolorize the blue starch/iodine complex. Calculate the molar concentration of the $\text{Na}_2\text{S}_2\text{O}_3$.

Solution

$$1 \text{ mol } \text{IO}_3^- = 6 \text{ mol } \text{S}_2\text{O}_3^{2-}$$

$$\text{amount } \text{Na}_2\text{S}_2\text{O}_3 = 0.1210 \text{ g } \text{KIO}_3 \times \frac{1 \text{ mmol } \text{KIO}_3}{0.21400 \text{ g } \text{KIO}_3} \times \frac{6 \text{ mmol } \text{Na}_2\text{S}_2\text{O}_3}{\text{mmol } \text{KIO}_3}$$

$$= 3.3925 \text{ mmol } \text{Na}_2\text{S}_2\text{O}_3$$

$$c_{\text{Na}_2\text{S}_2\text{O}_3} = \frac{3.3925 \text{ mmol } \text{Na}_2\text{S}_2\text{O}_3}{41.64 \text{ mL } \text{Na}_2\text{S}_2\text{O}_3} = 0.08147 \text{ M}$$

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TABLE 20-2 Some Applications of Sodium Thiosulfate as a Reductant		
Analyte	Half-Reaction	Special Conditions
IO_4^-	$\text{IO}_4^- + 8\text{H}^+ + 7\text{e}^- \rightleftharpoons \frac{1}{2}\text{I}_2 + 4\text{H}_2\text{O}$	Acidic solution
	$\text{IO}_4^- + 2\text{H}^+ + 2\text{e}^- \rightleftharpoons \text{IO}_3^- + \text{H}_2\text{O}$	Neutral solution
IO_3^-	$\text{IO}_3^- + 6\text{H}^+ + 5\text{e}^- \rightleftharpoons \frac{1}{2}\text{I}_2 + 3\text{H}_2\text{O}$	Strong acid
BrO_3^- , ClO_3^-	$\text{XO}_3^- + 6\text{H}^+ + 6\text{e}^- \rightleftharpoons \text{X}^- + 3\text{H}_2\text{O}$	Strong acid
Br_2 , Cl_2	$\text{X}_2 + 2\text{I}^- \rightleftharpoons \text{I}_2 + 2\text{X}^-$	
NO_3^-	$\text{HNO}_2 + \text{H}^+ + \text{e}^- \rightleftharpoons \text{NO}(g) + \text{H}_2\text{O}$	
Cu^{2+}	$\text{Cu}^{2+} + \text{I}^- + \text{e}^- \rightleftharpoons \text{CuI}(s)$	
O_2	$\text{O}_2 + 4\text{Mn(OH)}_2(s) + 2\text{H}_2\text{O} \rightleftharpoons 4\text{Mn(OH)}_3(s)$	Basic solution
	$\text{Mn(OH)}_3(s) + 3\text{H}^+ + \text{e}^- \rightleftharpoons \text{Mn}^{2+} + 3\text{H}_2\text{O}$	Acidic solution
O_3	$\text{O}_3(g) + 2\text{H}^+ + 2\text{e}^- \rightleftharpoons \text{O}_2(g) + \text{H}_2\text{O}$	
Organic peroxide	$\text{ROOH} + 2\text{H}^+ + 2\text{e}^- \rightleftharpoons \text{ROH} + \text{H}_2\text{O}$	

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Calculation Examples

1. Aqueous solutions containing approximately 3% (w/w) H₂O₂ are sold in drug stores as a disinfectant. A method for determining the peroxide content involves the use of 0.01145 M KMnO₄. Assume that you wish to use between 30 and 45 mL of the above KMnO₄ reagent for a titration. Calculate the amount of H₂O₂ needs to take.



The amount of KMnO₄ in 35 to 45 mL of the reagent is between

$$\begin{aligned}\text{amount KMnO}_4 &= 35 \text{ mL KMnO}_4 \times 0.01145 \frac{\text{mmol KMnO}_4}{\text{mL KMnO}_4} \\ &= 0.401 \text{ mmol KMnO}_4\end{aligned}$$

and

$$\text{amount KMnO}_4 = 45 \times 0.01145 = 0.515 \text{ mmol KMnO}_4$$

The amount of H₂O₂ consumed by 0.401 mmol of KMnO₄ is

$$\text{amount H}_2\text{O}_2 = 0.401 \text{ mmol KMnO}_4 \times \frac{5 \text{ mmol H}_2\text{O}_2}{2 \text{ mmol KMnO}_4} = 1.00 \text{ mmol H}_2\text{O}_2$$

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and

$$\text{amount H}_2\text{O}_2 = 0.515 \times \frac{5}{2} = 1.29 \text{ mmol H}_2\text{O}_2$$

We, therefore, need to take samples that contain from 1.00 to 1.29 mmol H₂O₂.

$$\begin{aligned}\text{mass sample} &= 1.00 \text{ mmol H}_2\text{O}_2 \times 0.03401 \frac{\text{g H}_2\text{O}_2}{\text{mmol H}_2\text{O}_2} \times \frac{100 \text{ g sample}}{3 \text{ g H}_2\text{O}_2} \\ &= 1.1 \text{ g sample}\end{aligned}$$

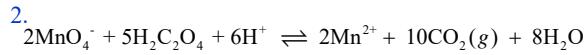
to

$$\text{mass sample} = 1.29 \times 0.03401 \times \frac{100}{3} = 1.5 \text{ g sample}$$

Thus, our samples should weigh between 1.1 and 1.5 g. These should be diluted to perhaps 75 to 100 mL with water and made slightly acidic with dilute H₂SO₄ before titration.

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The purity of a sample of sodium oxalate, Na₂C₂O₄, is determined by titrating with a standard solution of KMnO₄. If a 0.5116-g sample requires 35.62 mL of 0.0400 M KMnO₄ to reach the titration's end point, what is the %w/w Na₂C₂O₄ in the sample.



The moles of KMnO₄ used to reach the end point is

$$(0.0400 \text{ M KMnO}_4)(0.03562 \text{ L}) = 1.42 \times 10^{-3} \text{ mol KMnO}_4$$

which means the sample contains

$$1.42 \times 10^{-3} \text{ mol KMnO}_4 \times \frac{5 \text{ mol Na}_2\text{C}_2\text{O}_4}{2 \text{ mol KMnO}_4} = 3.55 \times 10^{-3} \text{ mol Na}_2\text{C}_2\text{O}_4$$

Thus, the %w/w Na₂C₂O₄ in the sample of ore is

$$3.55 \times 10^{-3} \text{ mol Na}_2\text{C}_2\text{O}_4 \times \frac{134.00 \text{ g Na}_2\text{C}_2\text{O}_4}{\text{mol Na}_2\text{C}_2\text{O}_4} = 0.476 \text{ g Na}_2\text{C}_2\text{O}_4$$

$$\frac{0.476 \text{ g Na}_2\text{C}_2\text{O}_4}{0.5116 \text{ g sample}} \times 100 = 93.0\% \text{ w/w Na}_2\text{C}_2\text{O}_4$$

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